

Limits Worksheet 1 Numerical and Graphically KEY

For questions 1 & 2, given the following find the limit numerically by completing the table.

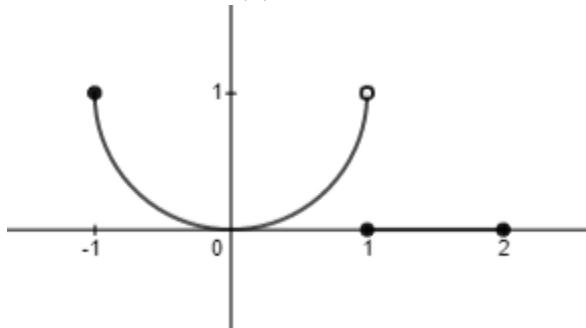
1) $\lim_{x \rightarrow -3} f(x) \frac{x+3}{x+3}$

x	-3.1	-3.01	->-3<-	-2.99	-2.9
f(x)	1	1	1	1	1

2) $\lim_{x \rightarrow 1} f(x) \frac{x-1}{x^2-1} = \lim_{x \rightarrow 1} f(x) \frac{x-1}{(x-1)(x+1)} = \lim_{x \rightarrow 1} f(x) \frac{1}{(x+1)}$

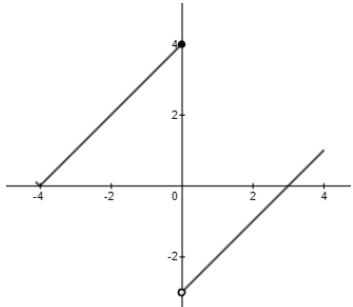
x	0.99	0.999	->1<-	1.001	1.01
f(x)	0.5025	0.5002	0.5	0.4998	4.975

3) Given the graph $y = f(x)$ below state whether the following are true or false.



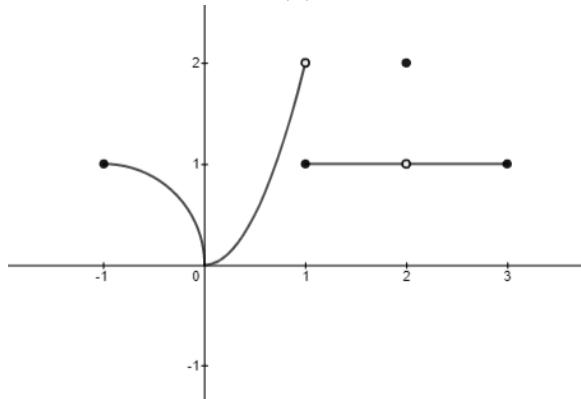
- a) $\lim_{x \rightarrow -1^-} f(x) = 1$ b) $\lim_{x \rightarrow 0^-} f(x) = 1$ c) $\lim_{x \rightarrow 0} f(x)$ exists d) $\lim_{x \rightarrow 0} f(x) = 1$
TRUE **FALSE** **TRUE** **FALSE**
- e) $\lim_{x \rightarrow 1} f(x) = 0$ f) $\lim_{x \rightarrow 0^-} f(x) = 0$ g) $\lim_{x \rightarrow 0^-} f(x) = \lim_{x \rightarrow 0^+} f(x)$ h) $\lim_{x \rightarrow 0} f(x) = 0$
FALSE **TRUE** **TRUE** **TRUE**
- i) $\lim_{x \rightarrow 1} f(x) = 1$ j) $\lim_{x \rightarrow 2^-} f(x) = 2$
FALSE **FALSE**

4) Given the graph $y = F(x)$ below, find



- a) $\lim_{x \rightarrow 0^-} F(x) = 4$ b) $\lim_{x \rightarrow 0^+} F(x) = -3$ c) $\lim_{x \rightarrow 0} F(x)$ DNE d) $F(0) = 4$

5) Given the graph $y = f(x)$ below, determine if the following are TRUE or FALSE.



a) $\lim_{x \rightarrow -1^+} f(x) = 1$
TRUE

b) $\lim_{x \rightarrow 2} f(x) = \text{does not exist}$
FALSE

c) $\lim_{x \rightarrow 2} f(x) = 2$
FALSE

d) $\lim_{x \rightarrow 1^-} f(x) = 2$
TRUE

e) $\lim_{x \rightarrow 1^+} f(x) = 1$
TRUE

f) $\lim_{x \rightarrow 1} f(x) = \text{DNE}$
TRUE

g) $\lim_{x \rightarrow 0^-} f(x) = \lim_{x \rightarrow 0^+} f(x)$
TRUE

h) $\lim_{x \rightarrow c} f(x)$ exists at every c in $(-1, 1)$
TRUE

i) $\lim_{x \rightarrow c} f(x)$ exists at every c in $(1, 3)$
TRUE

6) Given the graph $y = p(x)$ below find

a) $\lim_{x \rightarrow -2^-} p(x) = 3$

b) $\lim_{x \rightarrow -2^+} p(x) = 3$

c) $\lim_{x \rightarrow -2} p(x) = 3$

d) $p(-2) = 3$

